

**Space Geodesy:
for COSMIC and using COSMIC**

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[C.W. Hwang, E. Pavlis, C.K. Shum, C.L.Tseng, M. Yang]

J_2 (Earth's oblateness)

- by far the largest gravity “anomaly”
- $\sim 100\%$ due to rotational equilibrium
- $= 0.0010826265\dots$
- corresponds to a geoid “flattening” $\sim 1/300$
 - \sim centrifugal force / gravity
 - \sim equatorial bulge / Earth radius
- varies at and beyond the last digit, due to geophysical and climatic mass redistributions.

Sputnik 1, 1957



The plane of the satellite orbit remains fixed in space (except for the effects of perturbations) while the earth turns on its axis within the orbit. These diagrams, based on releases from Moscow, show every third circuit of the first artificial satellite, over Russia, western Africa, United States, the eastern Pacific Ocean, and China.

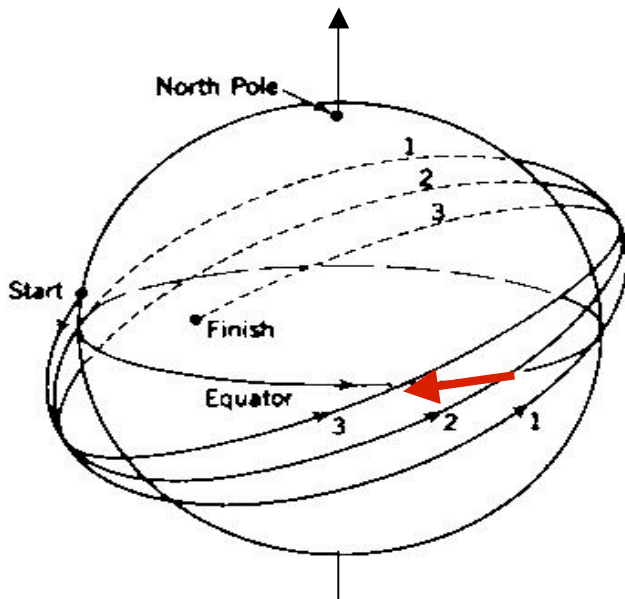
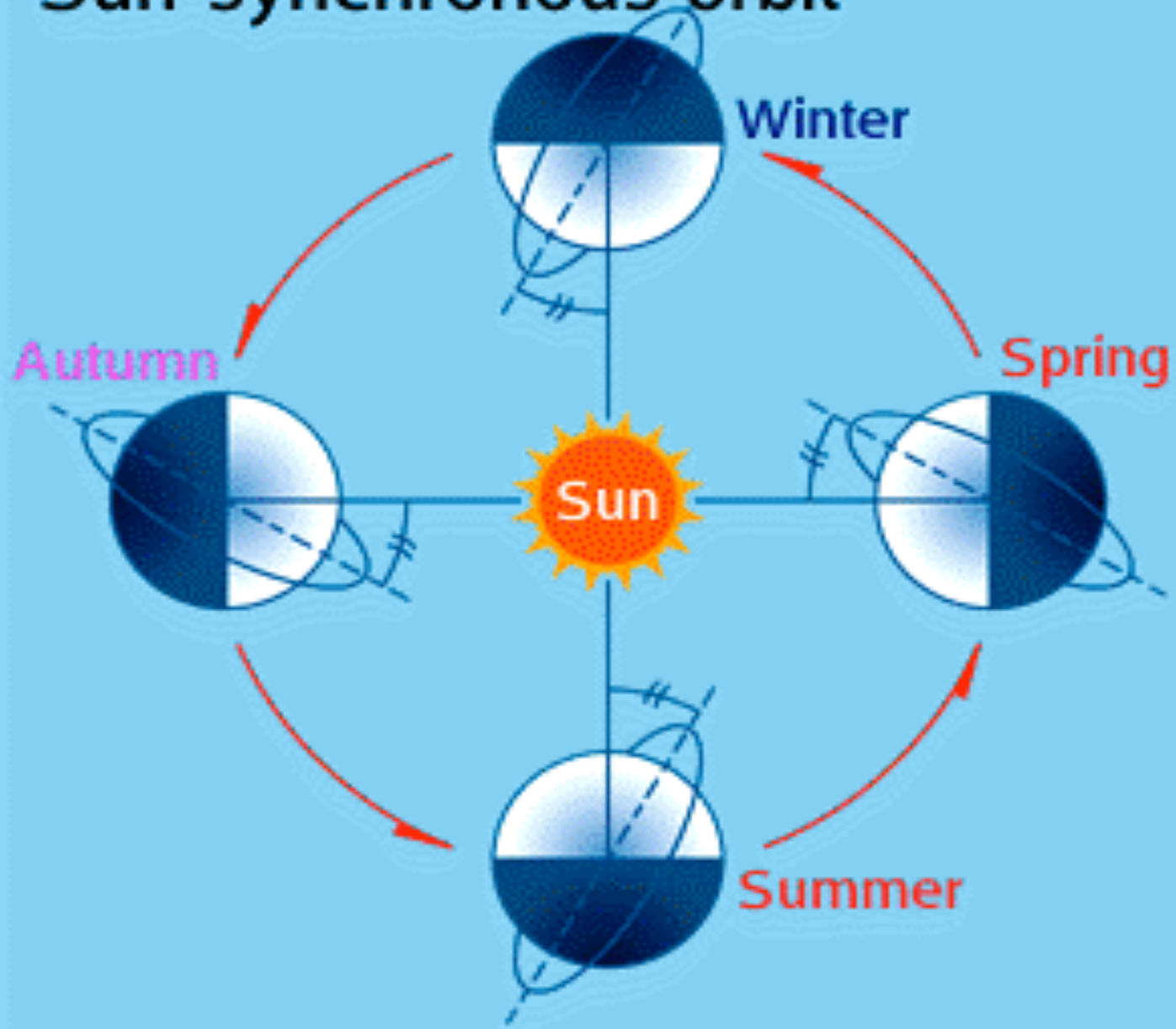


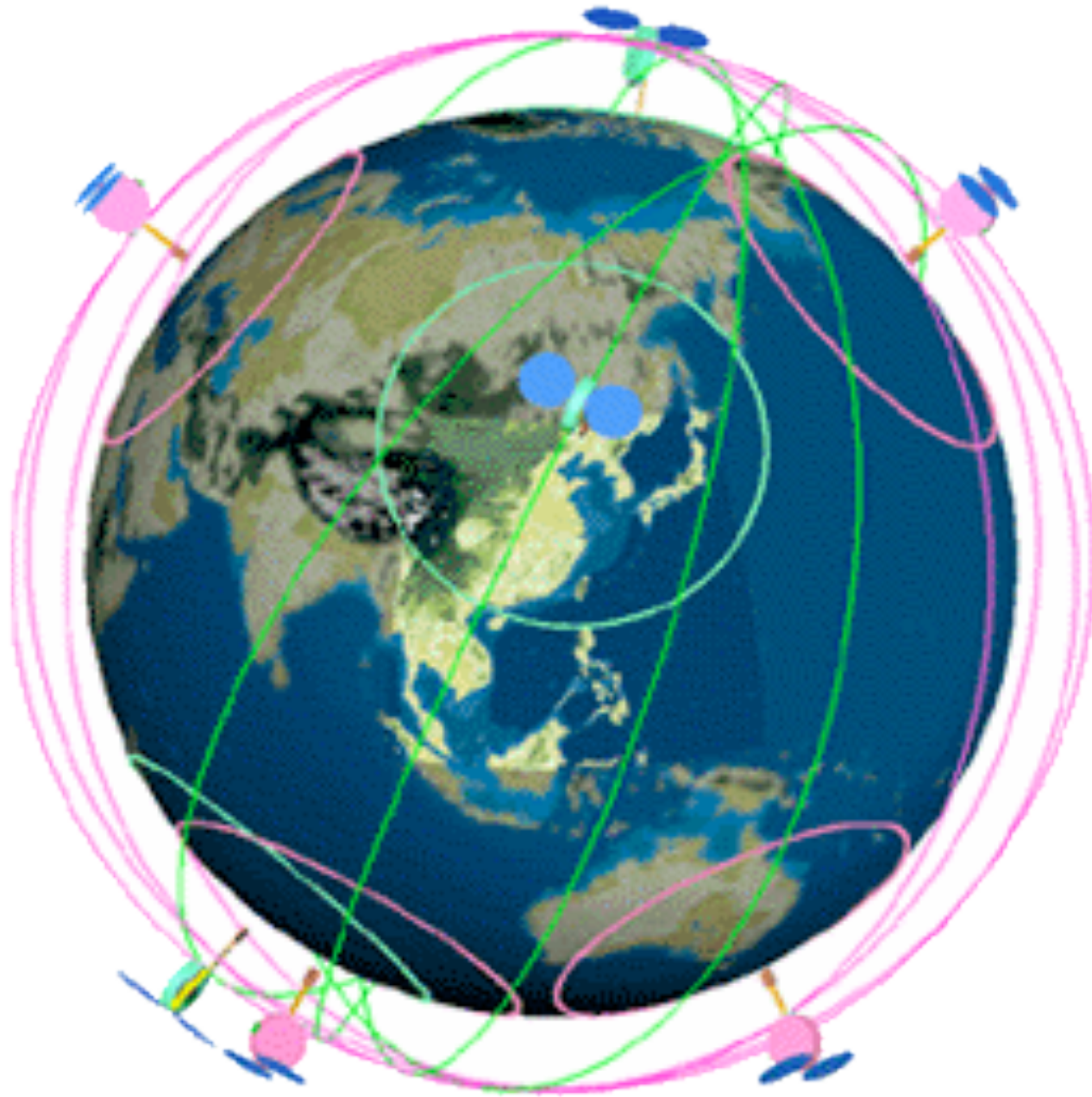
Figure 5-11 The regression of the nodes.

Satellite nodal precession
(around an oblate Earth)

→ Orbits separation of
COSMIC satellites at
different altitudes

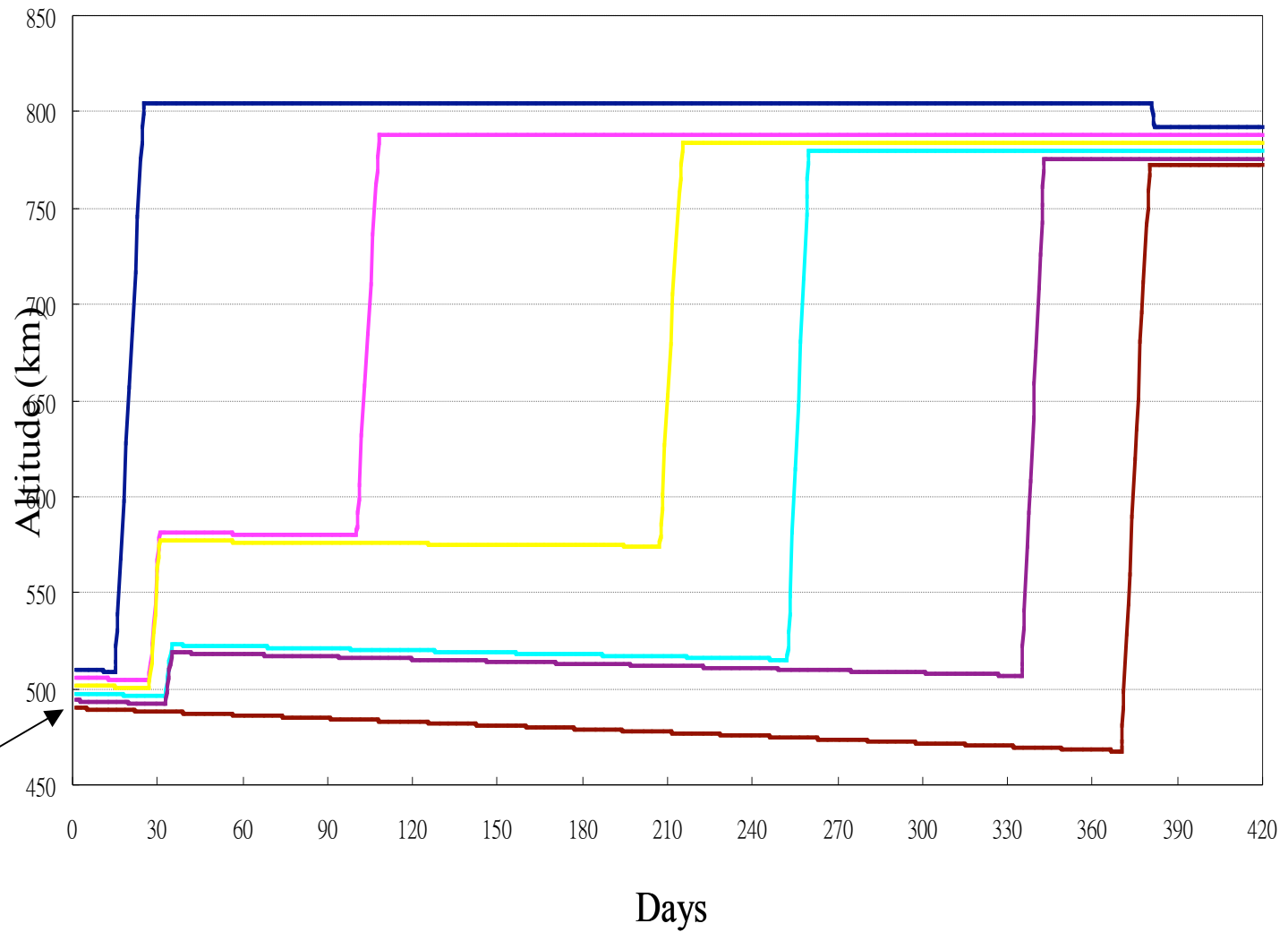
Sun-synchronous orbit





COSMIC
constellation:
6 satellites
6 orbits:
800 km altitude
71° inclination

COSMIC Constellation (6 satellites) Deployment Phase



one
launch

Space geodesy for COSMIC and using COSMIC

- COSMIC needs space geodesy
 - precise orbit/timing for GPS constellation (IGS)
 - precise orbit/timing for COSMIC LEO constellation (COSMIC Project)
 - NASA's Space Geodesy program provides the precise GPS technology, making GPS into a precise geodetic tool
 - "COSMIC IS a space geodetic mission!"

Space geodesy for COSMIC and using COSMIC

- COSMIC can benefit space geodesy
 - LEO orbits can solve for gravity, especially time-variable gravity during the mission lifetime (a “by product!”)
 - an active NASA research interest in space geodesy (e.g., GRACE mission)
 - better determination of GPS constellation orbit
 - better determination of lower-atmosphere pressure (supporting studies of time-variable gravity, Earth rotation variation, altimetry,...)

Measuring Gravity

- Surface
 - centrifugal (pseudo-)force correction
 - free-air anomaly
 - Bouguer anomaly
- Air-borne, Ship-borne
 - centrifugal (pseudo-)force correction
 - Coriolis (pseudo-)force correction (Eötvös effect)
 - platform acceleration (“noise”)
- Space-born
 - gravity canceled by centrifugal force (free fall)

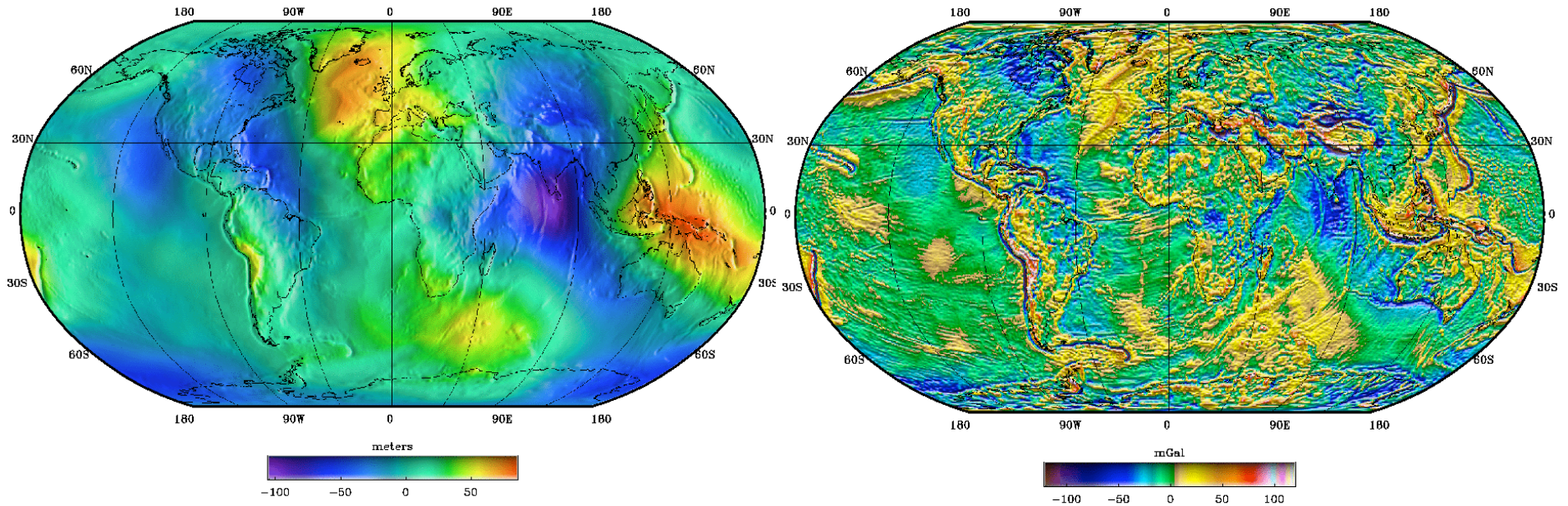
“Measuring” Gravity from Space

- Space-borne gravimeter won't work! (free fall)
- Gravity gradiometer --- GOCE (2003)
- Low-Earth orbit (LEO) satellite's precise orbit determination (POD)
 - Ground tracking for >4 decades (since Sputnik 1!)
 - positioning, range, Doppler/range-rate
 - Optical, radio, laser
 - Satellite-to-satellite tracking
 - “high-low” (GPS-LEO): CHAMP (2000), GRACE (2002), GOCE, **COSMIC**, altimeter missions, many future ones....
 - “low-low” (LEO-LEO): GRACE, Follow-ons
 - Need to correct for non-gravitational forces (air drag, radiation pressure)
 - on-board accelerometer (CHAMP, GRACE)
 - “drag-free”/proof mass system (GOCE, GP-B)
 - modeling: past ones, **COSMIC**.
 - common-mode cancellation (e.g., tandem constellation): **COSMIC**
 - smaller surface-to-mass ratio always helps
- Additional information (for geoid) provided by ocean altimetry and surface gravity

“Measuring” Gravity from Space : Milestones

- 1957 Sputnik 1 – J_2 (Earth oblateness)
- Kaula’s (1966) theory (spherical harmonics)
- Early 1970s, Satellite-laser-ranging
- Spherical harmonic solutions
 - ~1970s, 10 x 10
 - ~1980s, 36 x 36, 70 x 70
 - ~1990s, 180 x 180, 360 x 360
- **time-variable**: “ J_2 dot” (1980s)
- **time-variable**: J_2 and low-degree variations (1990s)
- CHAMP (2000), **GRACE (2002)**, GOCE (2006) +...
- **What about COSMIC?**

Static Gravity Field

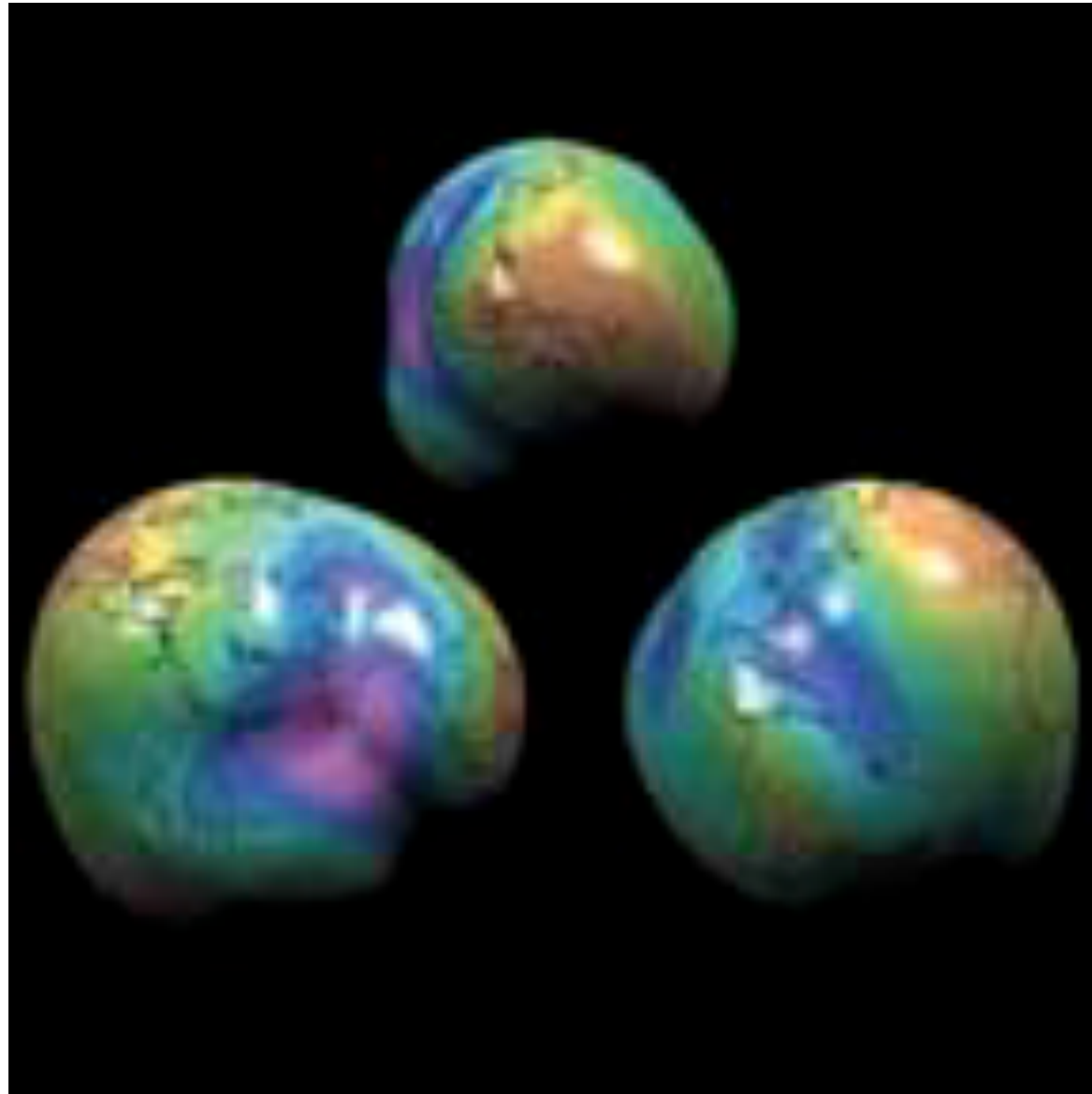


Geoid

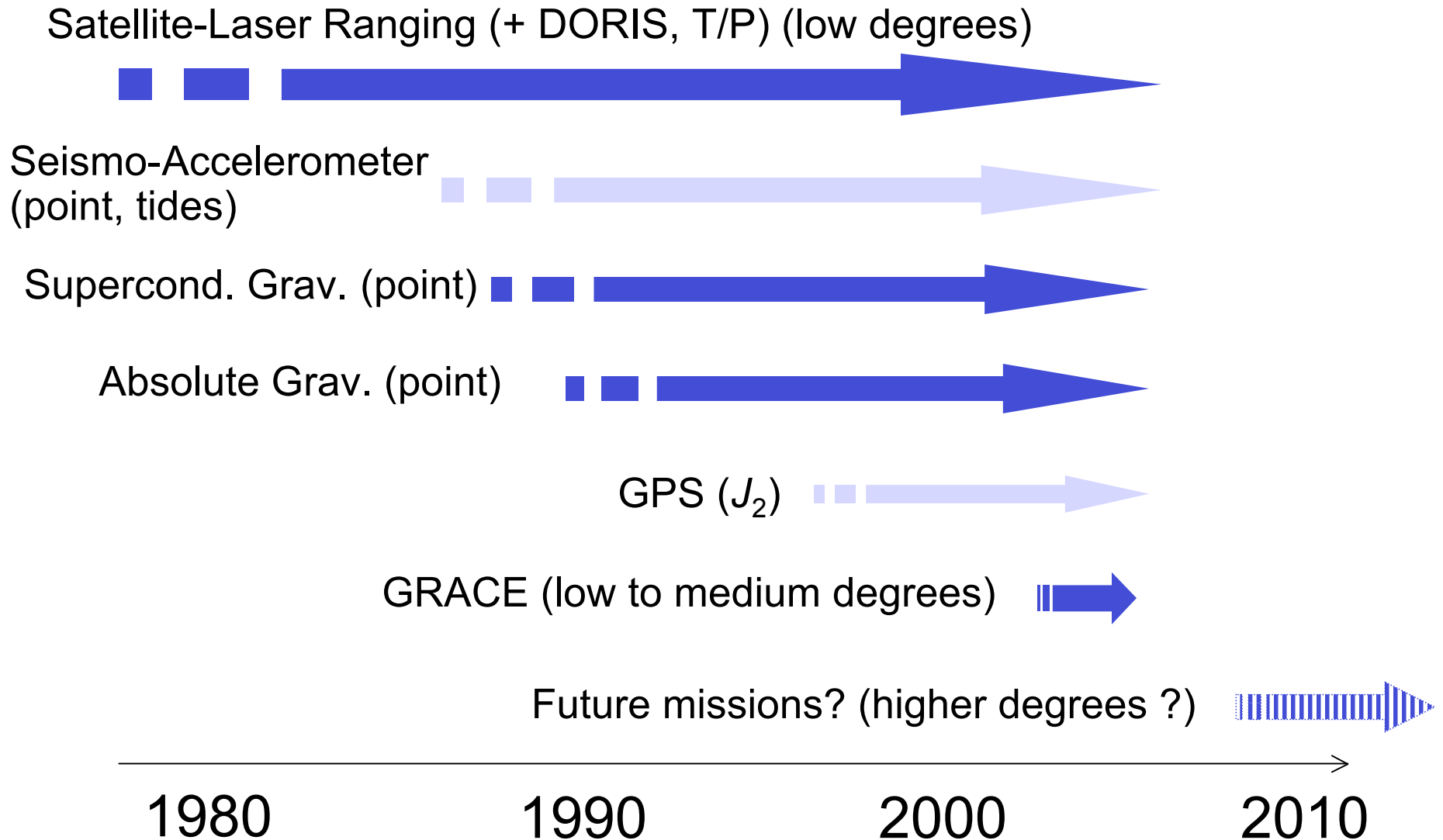
Gravity Anomaly

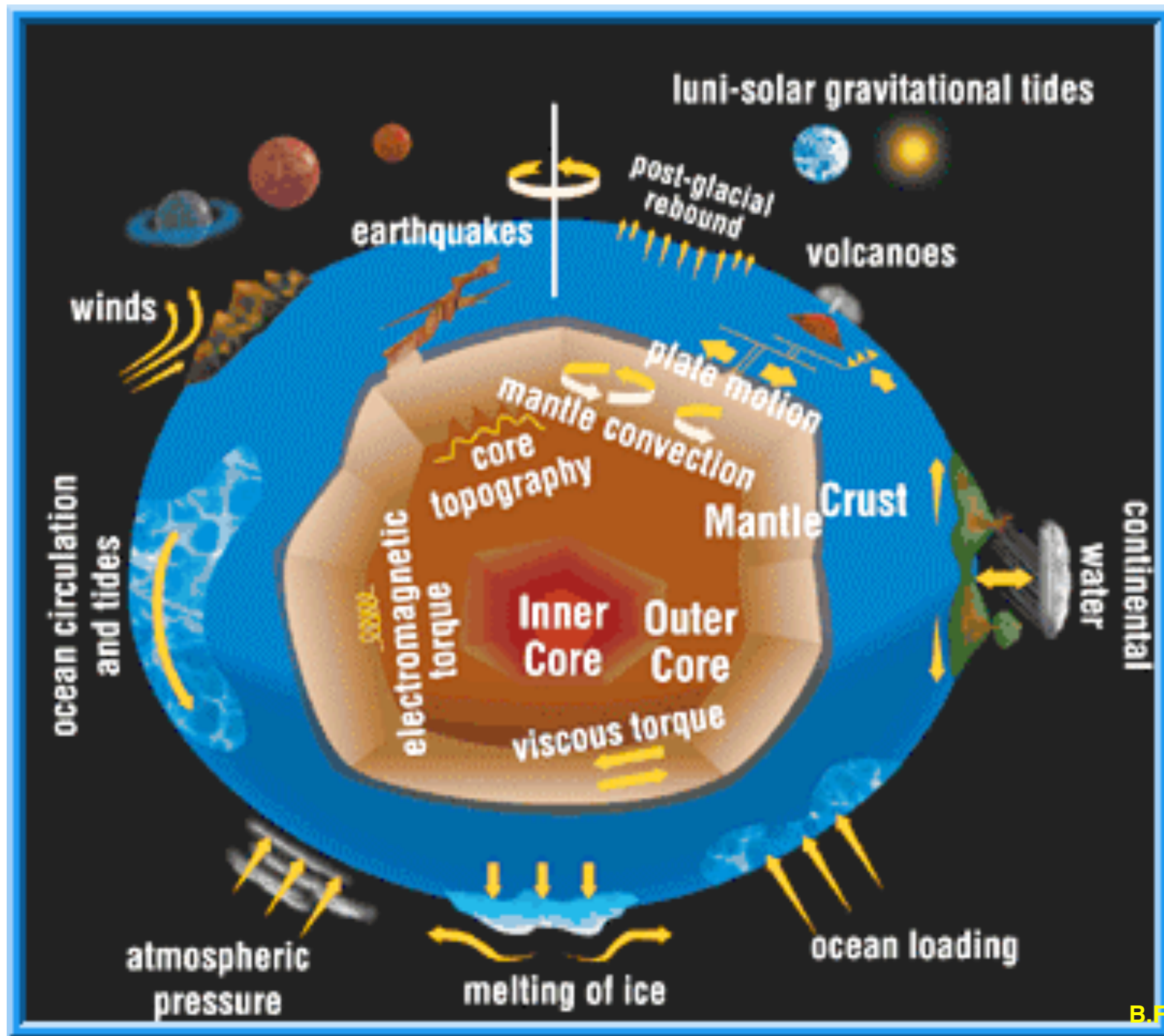
EGM96

Earth's Geoid (equi-potential surface) Model

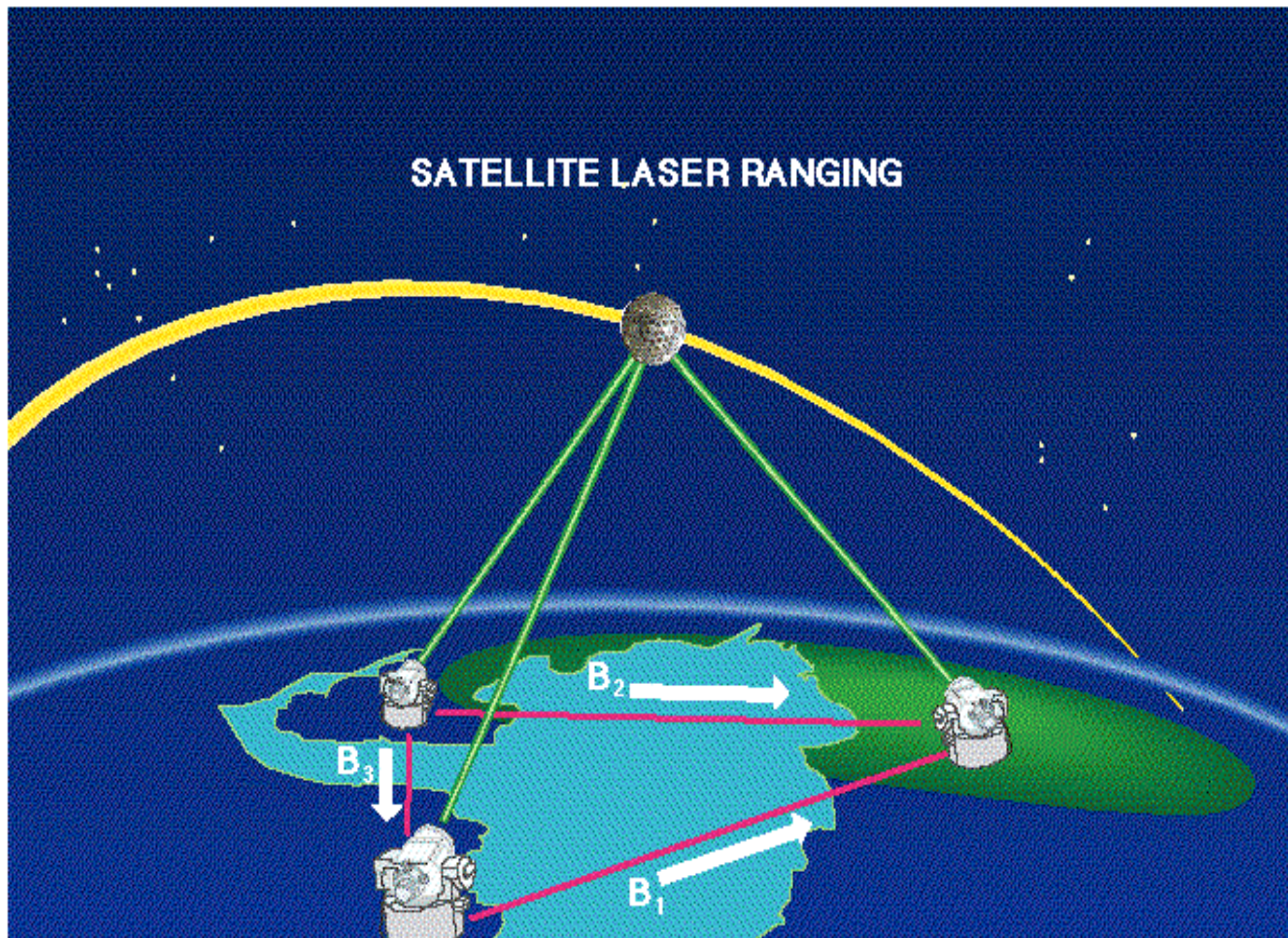


Time-Variable Gravity Observations





SATELLITE LASER RANGING



INTERNATIONAL SLR NETWORK

30 COUNTRIES—43 STATIONS

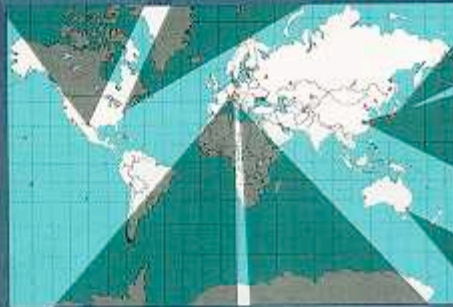
McDonald Observatory, Texas



Greenbelt, Maryland



Simosato, Japan



Shanghai, China



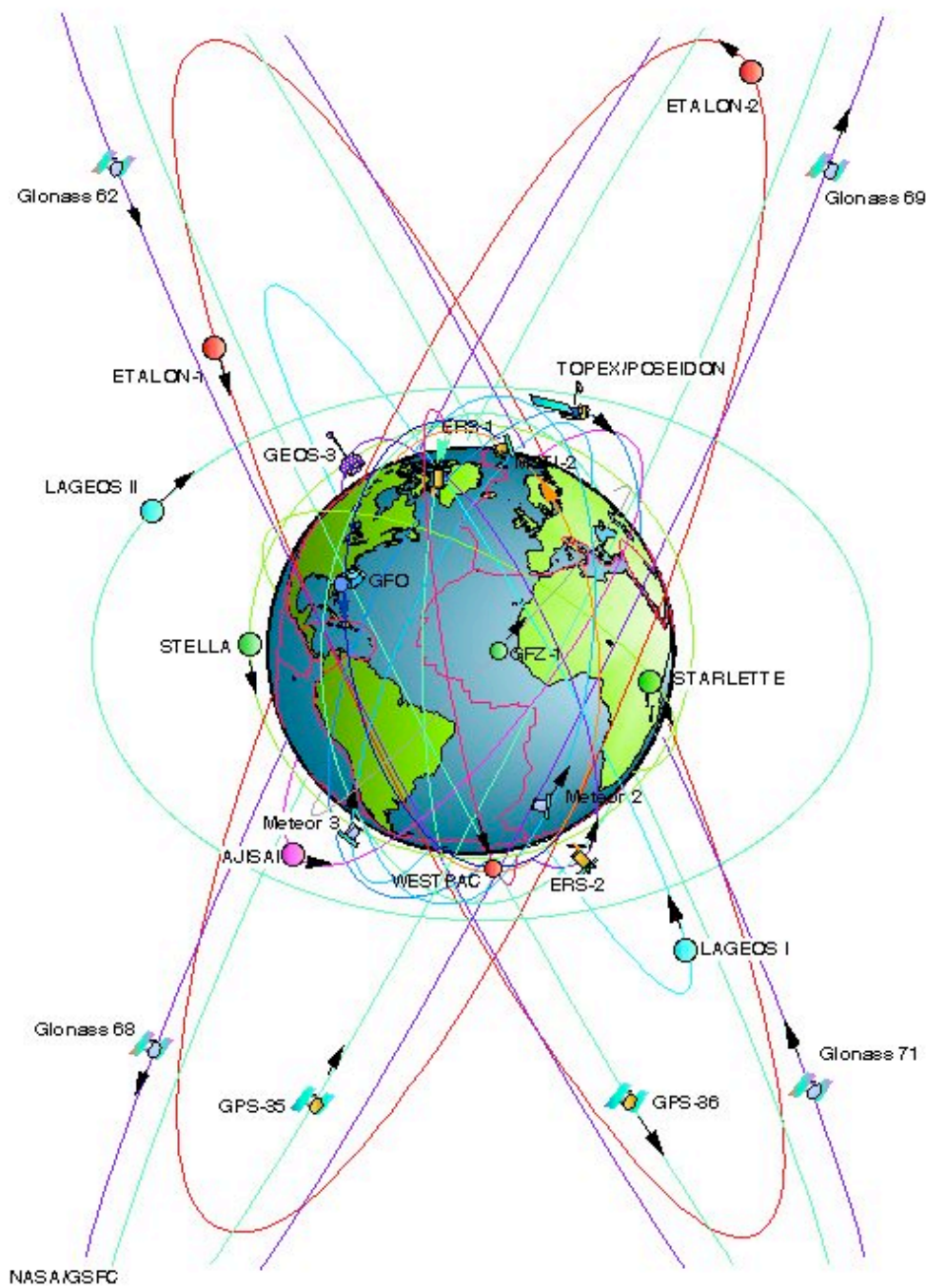
Wettzell, Germany



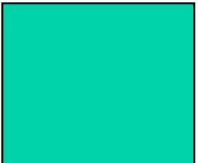
Matera, Italy



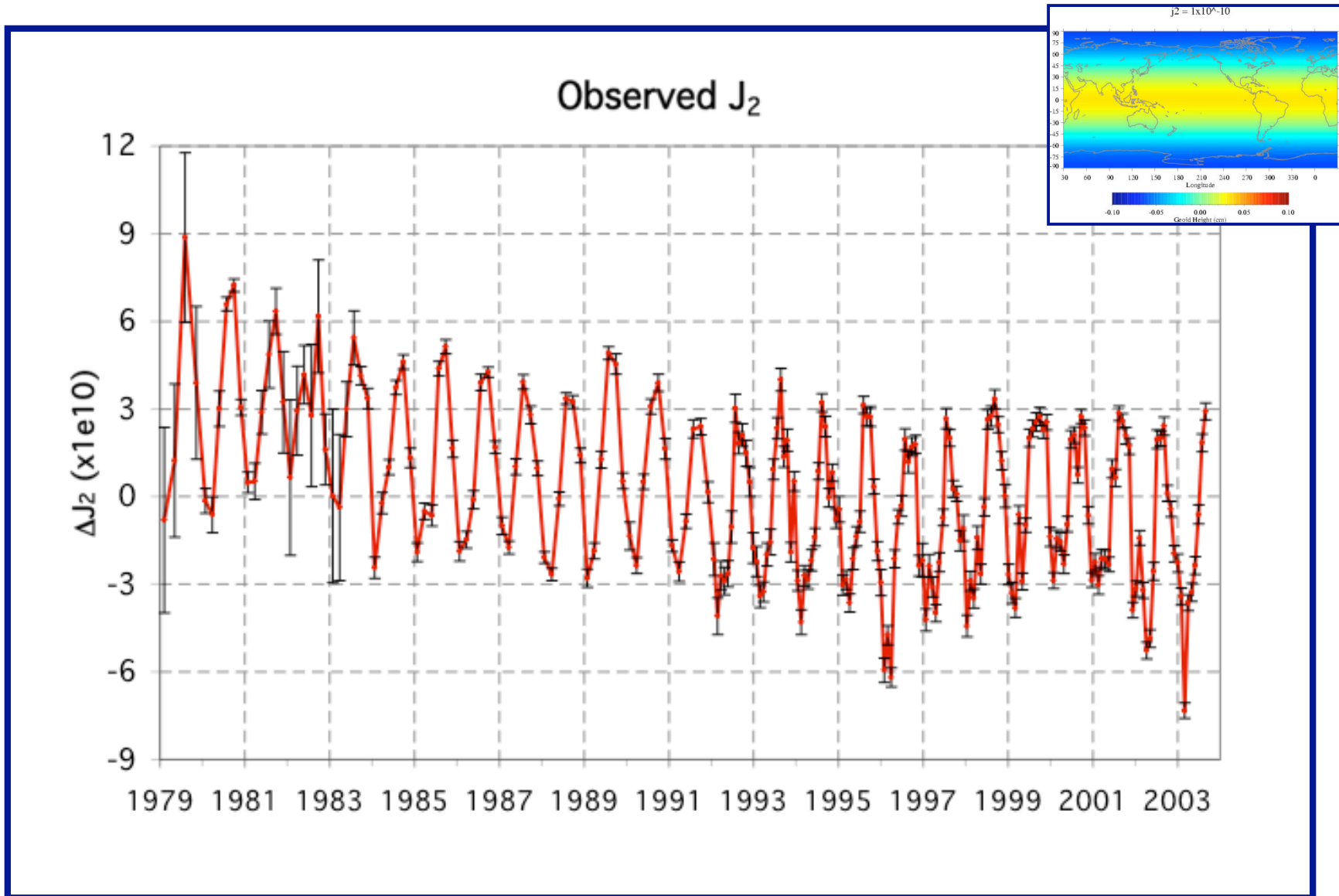
Ororal, Australia



Satellites tracked by the Laser Ranging network (in addition to the Moon)

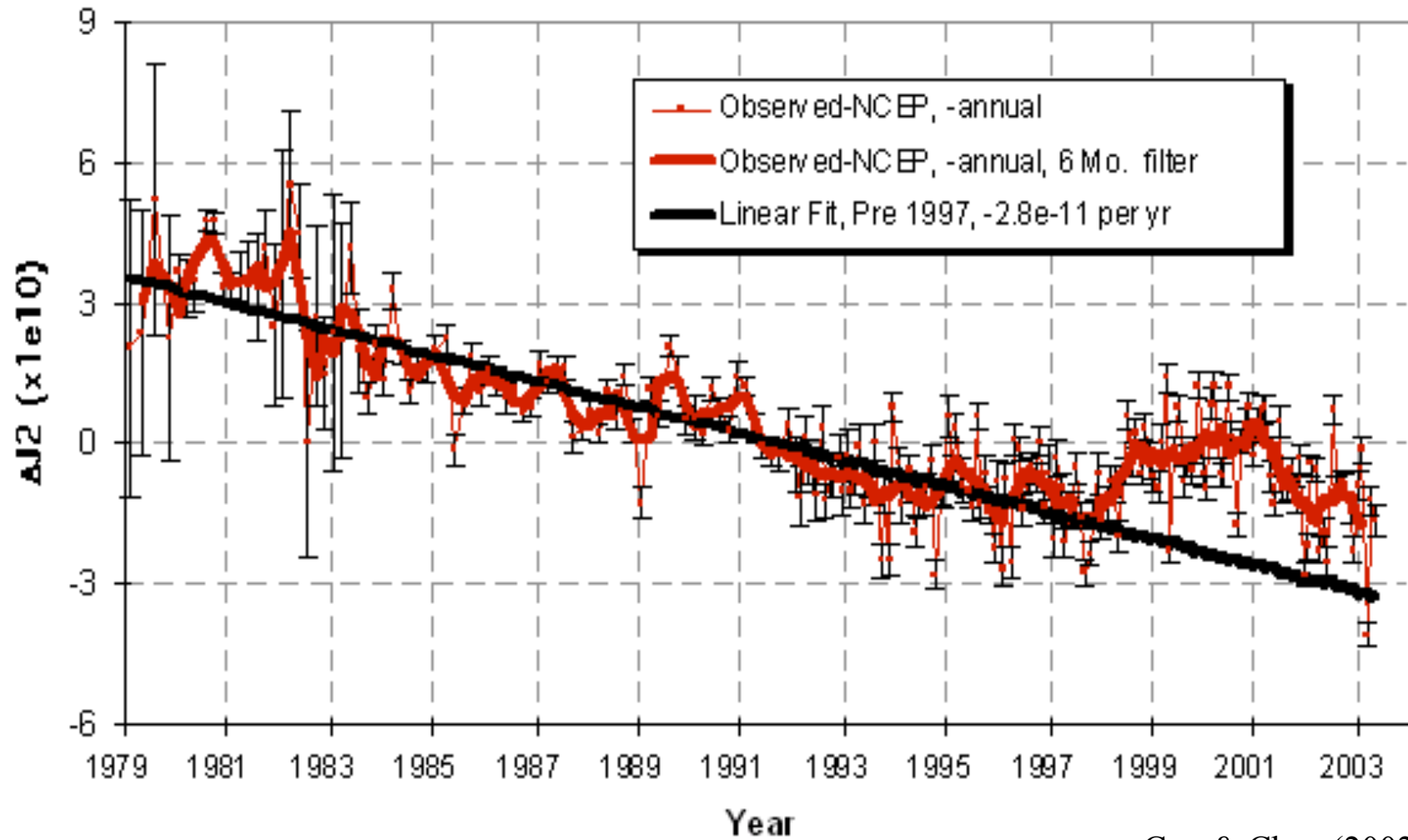


SLR Observed Earth oblateness J_2

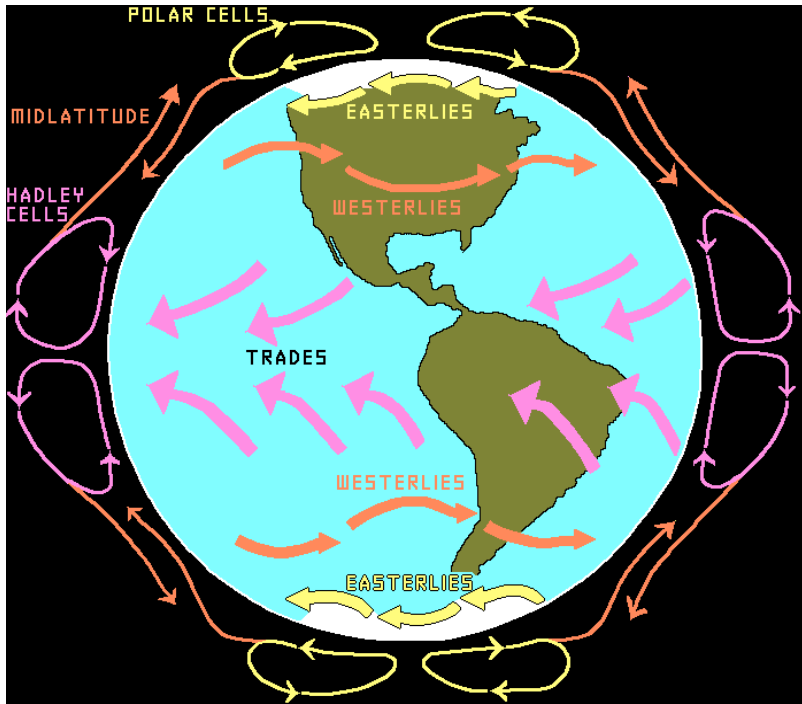


SLR observed J_2

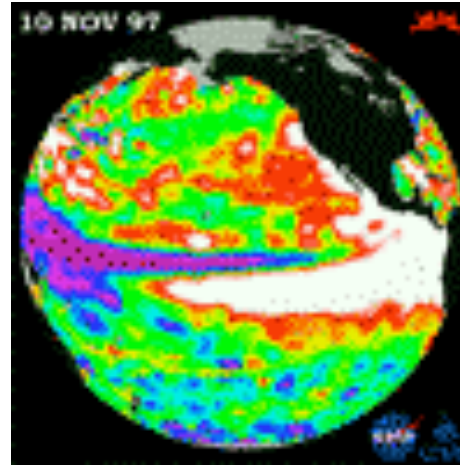
(non-seasonal, non-atmosphere, non-tidal)



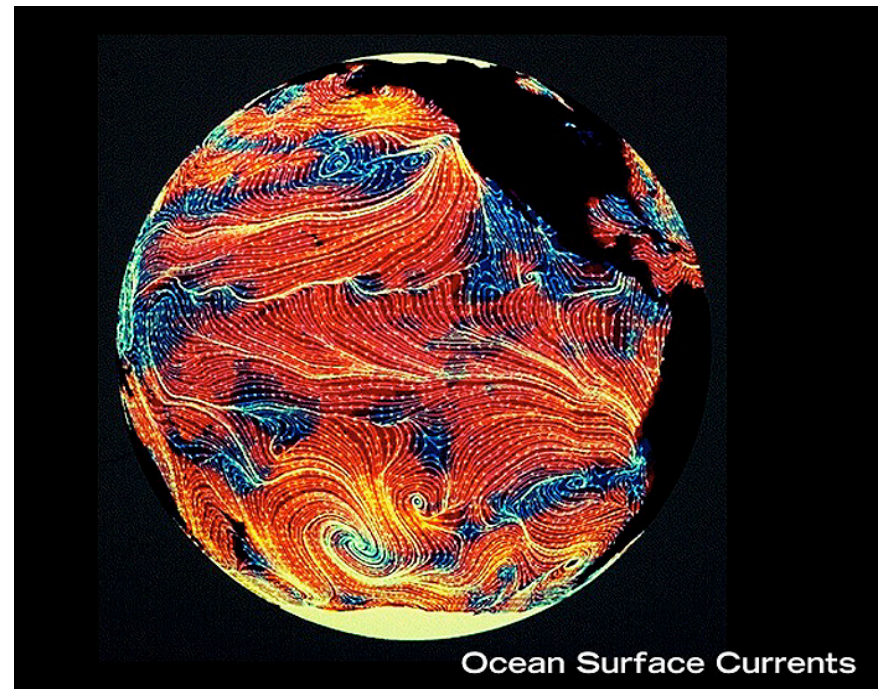
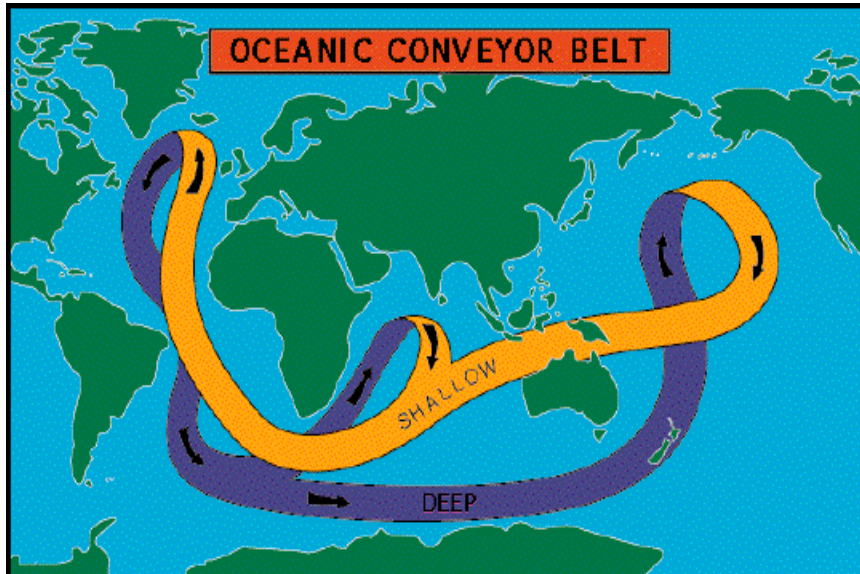
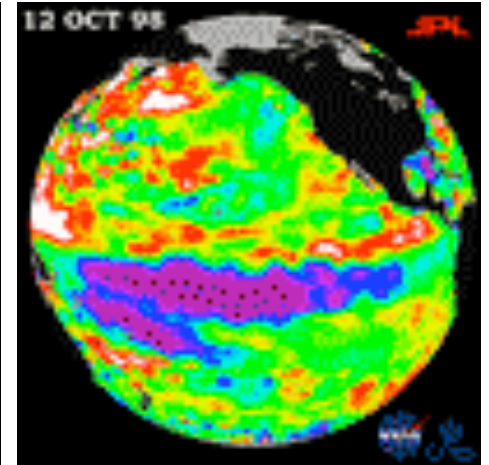
Cox & Chao (2002)



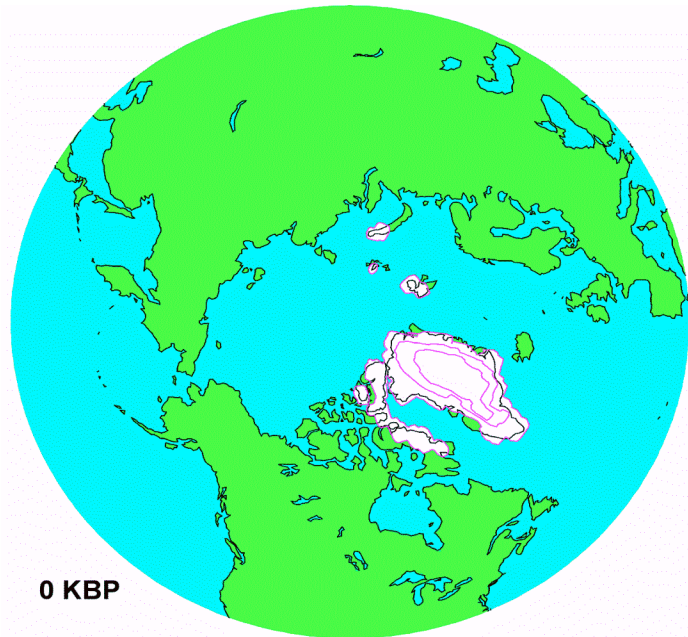
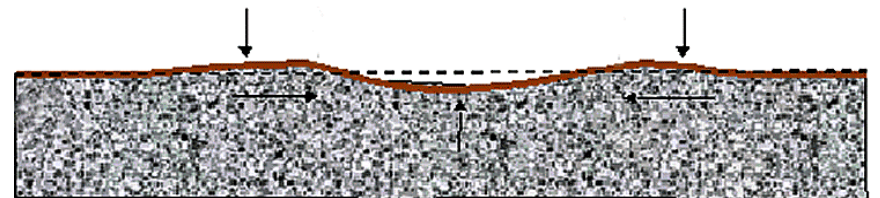
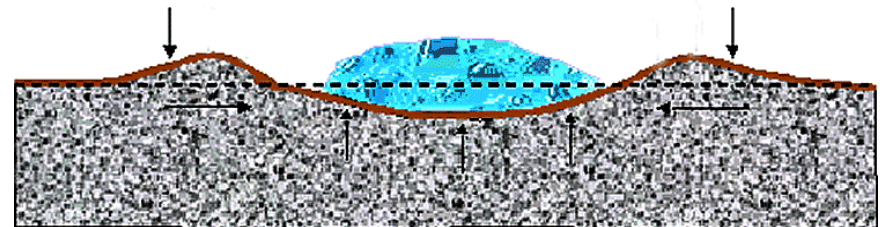
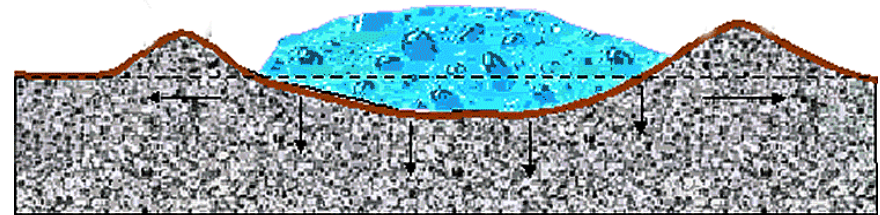
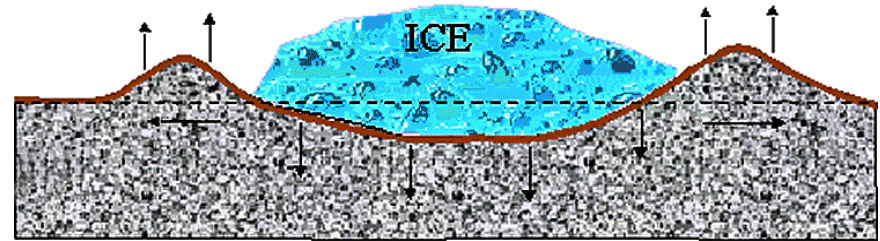
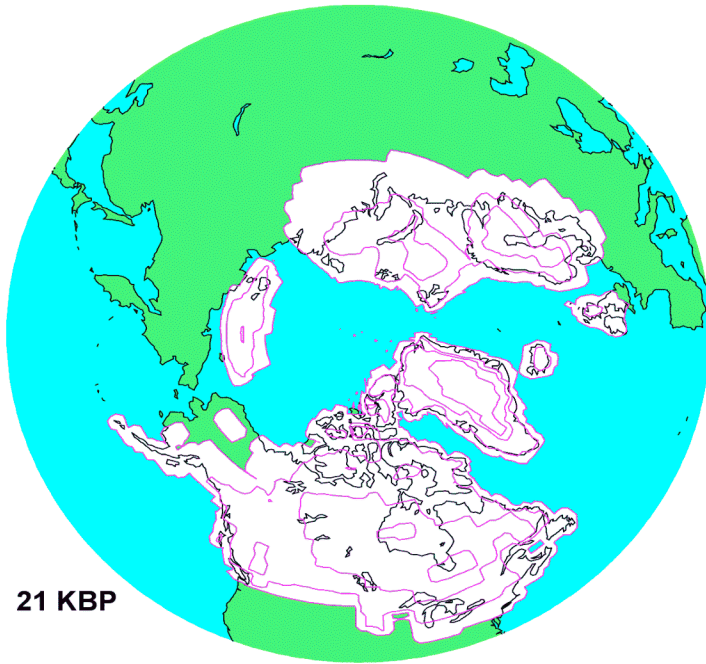
El Niño (11/1997)



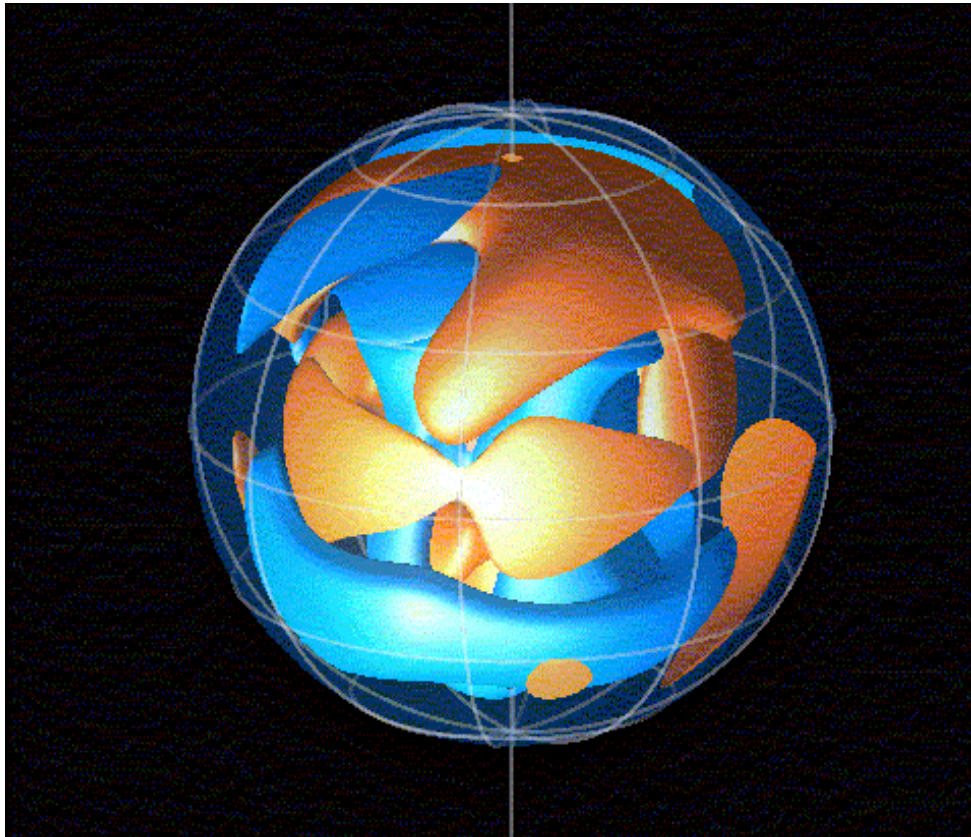
La Niña (10/1998)



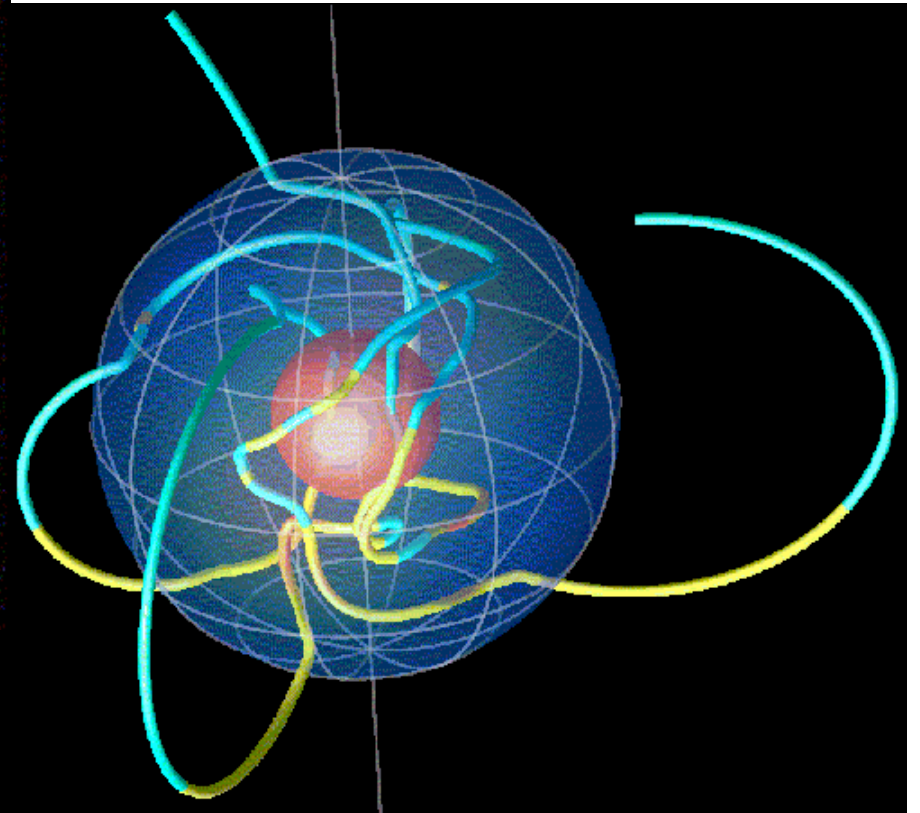
Since the peak of last great ice age, 20K years ago...

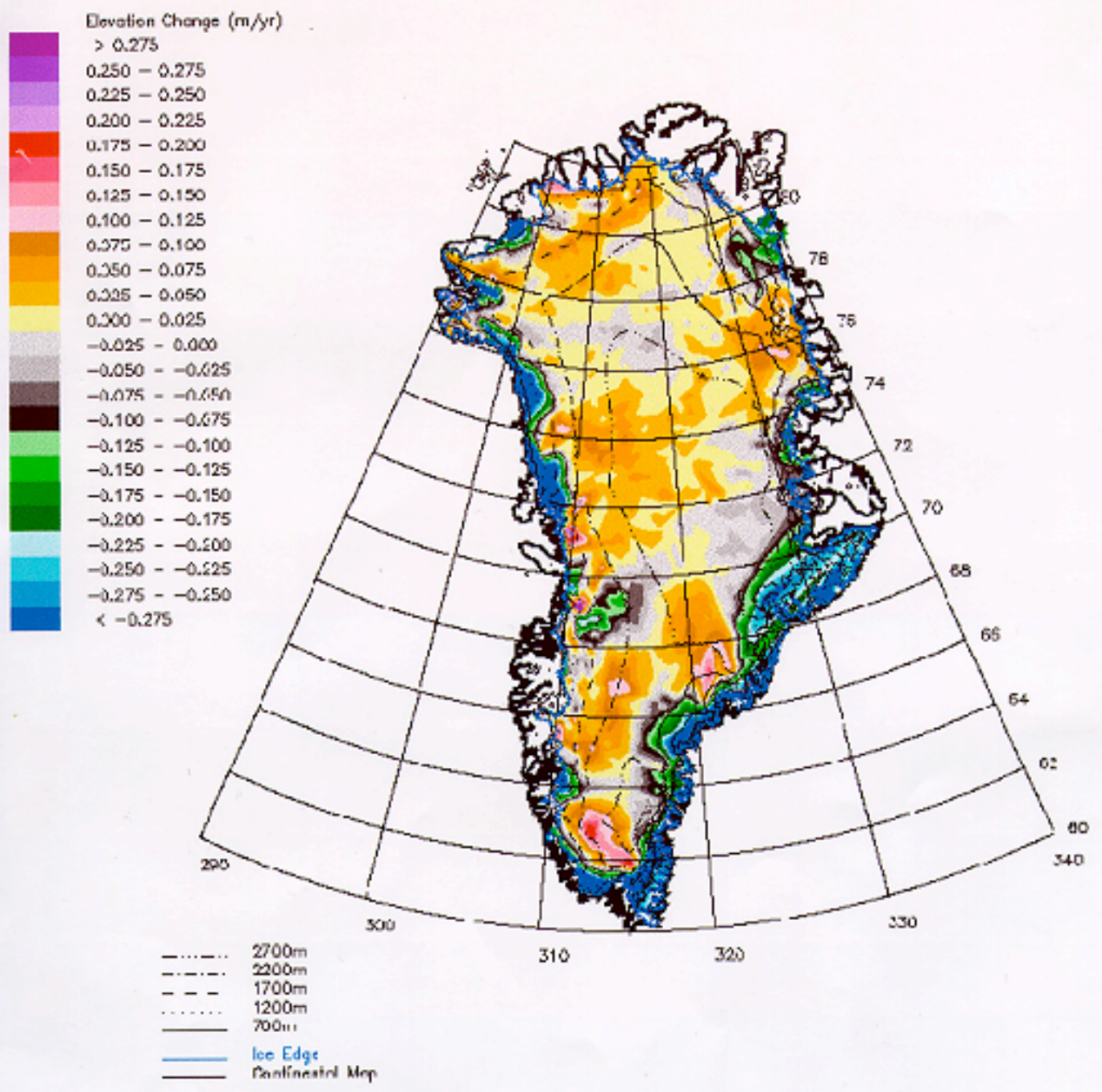


Fluid Core Motions and Geomagnetic Field



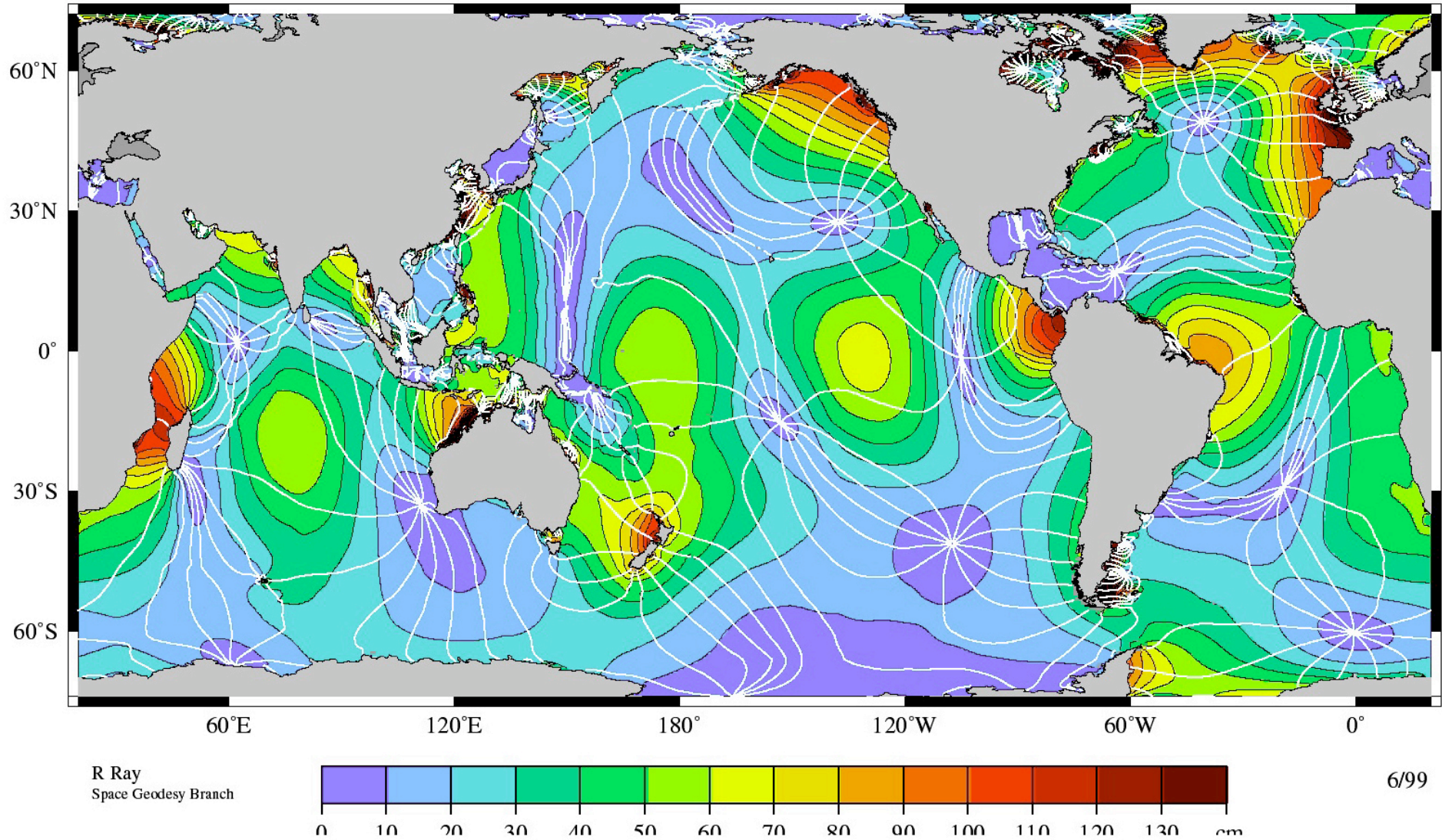
MoSST geodynamo model



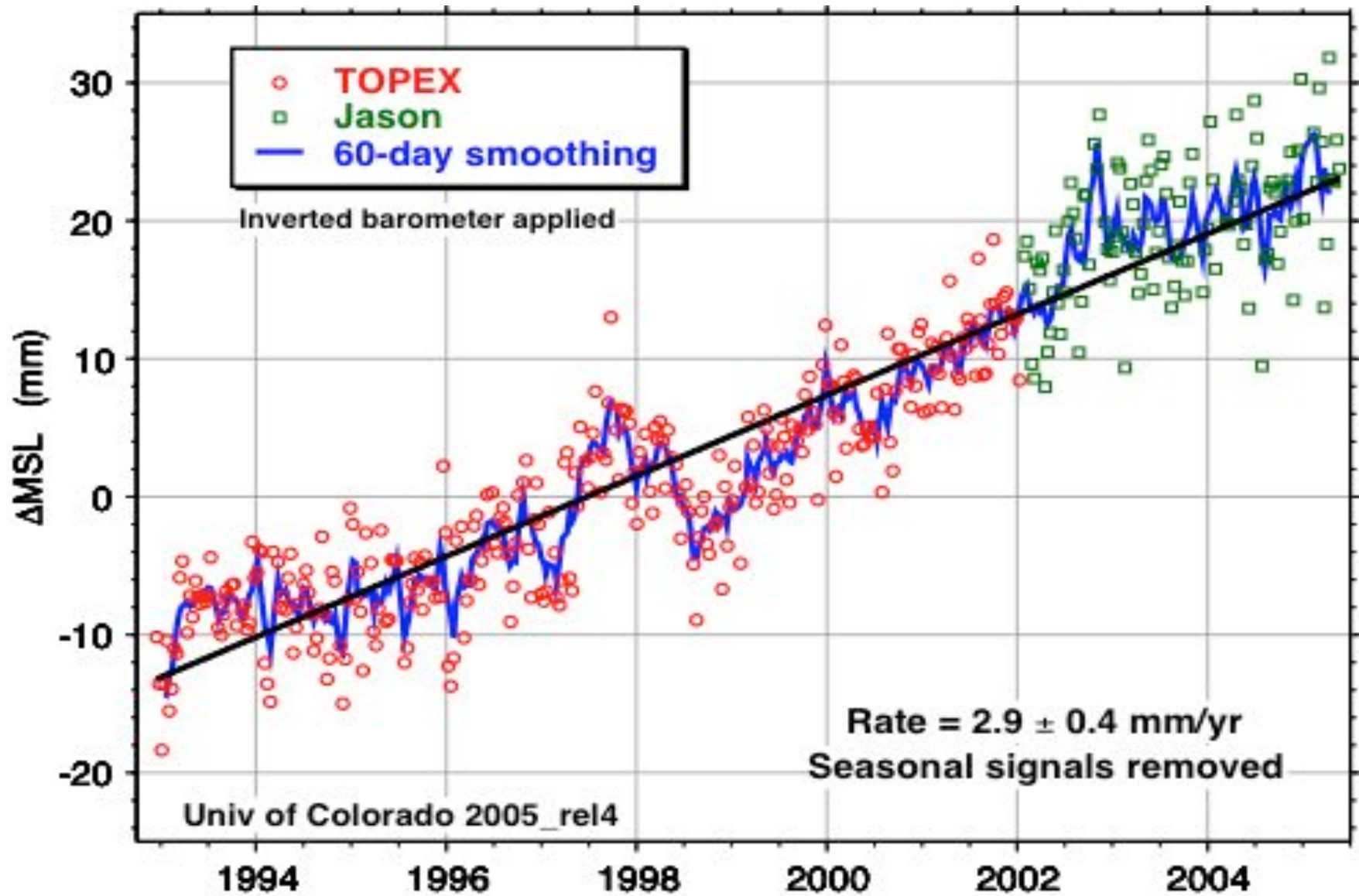




M₂ Lunar Tide in the Ocean



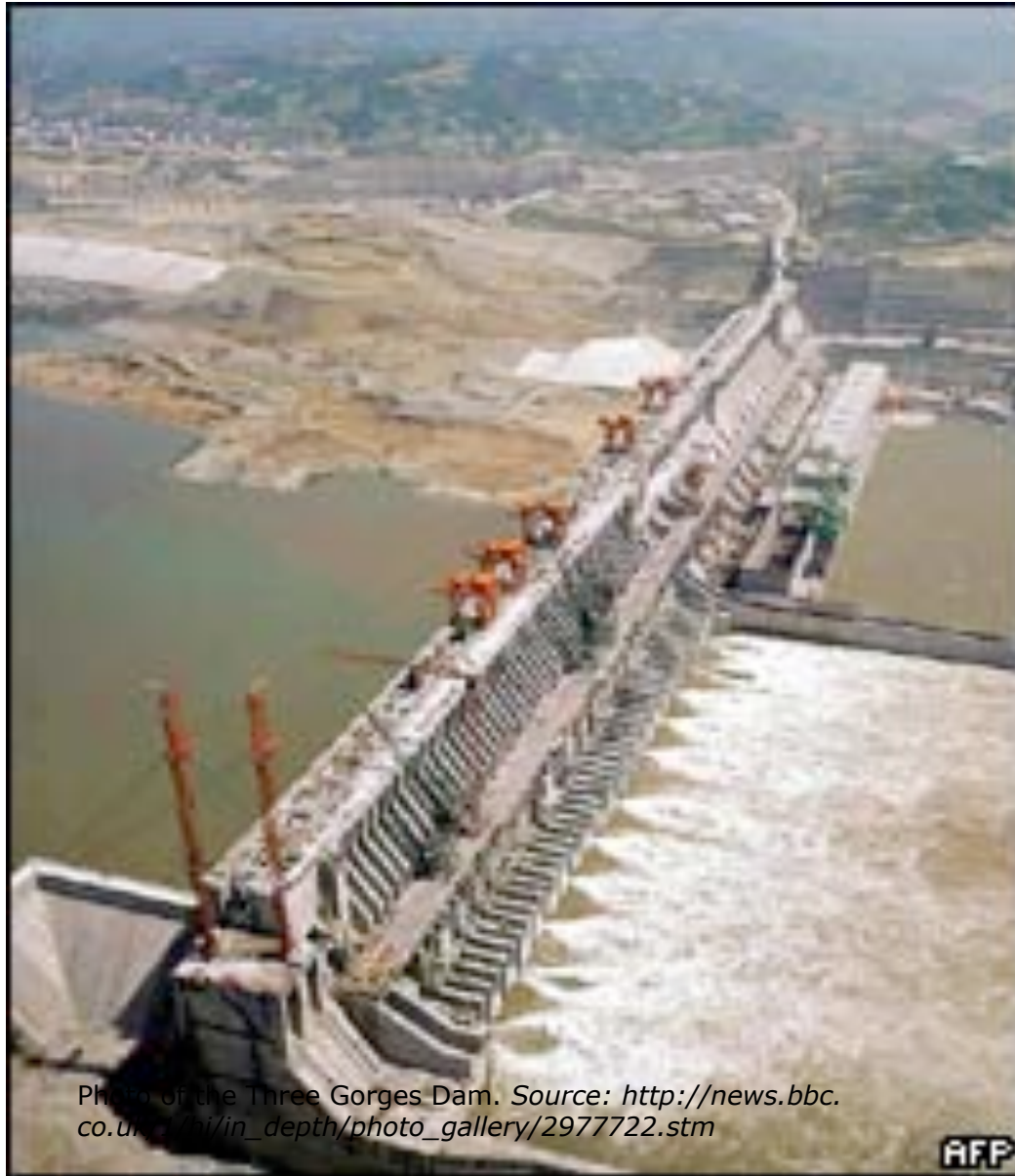
(GOT99, courtesy R. Ray)



Global Sea Level Rise From Topex/Poseidon

(courtesy S. Nerem)

The Three-Gorges Dam Project



History:

Dr. Sun Yatsen, 1917

Savage Report, 1940s

Debates in 1950-60s

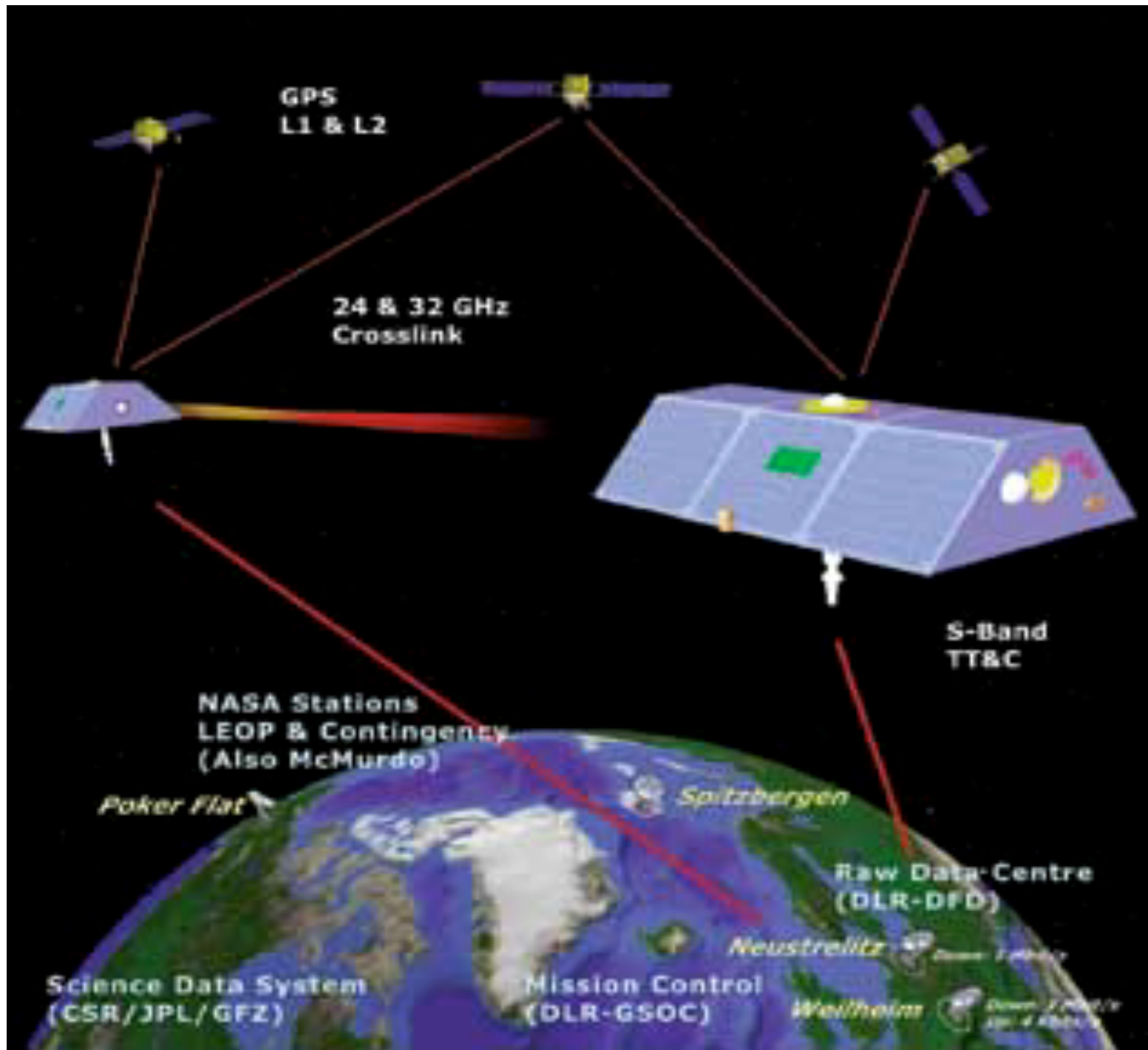
GeZhouBa Project, 1981

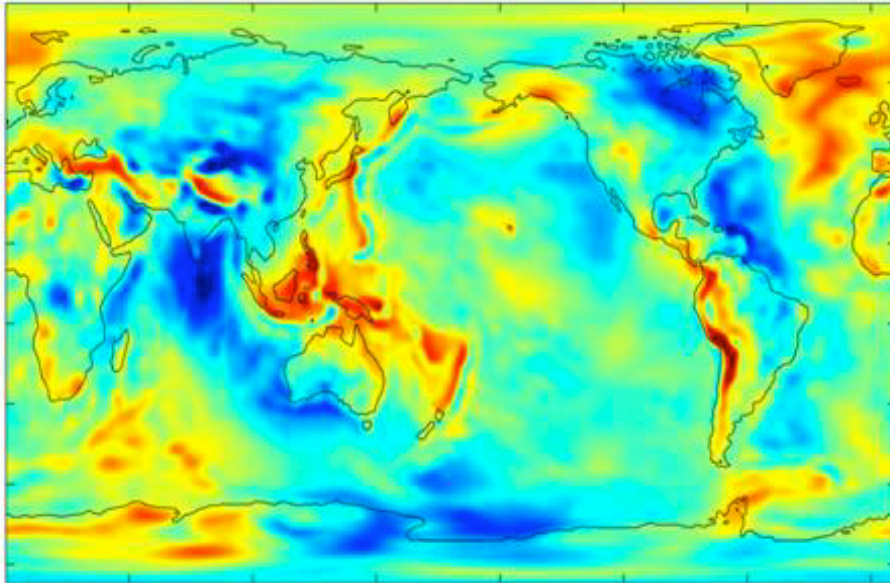
Three-Gorges Dam decided in 1992.

Phase 1 (1993-1997): Block the river and divert the flow.

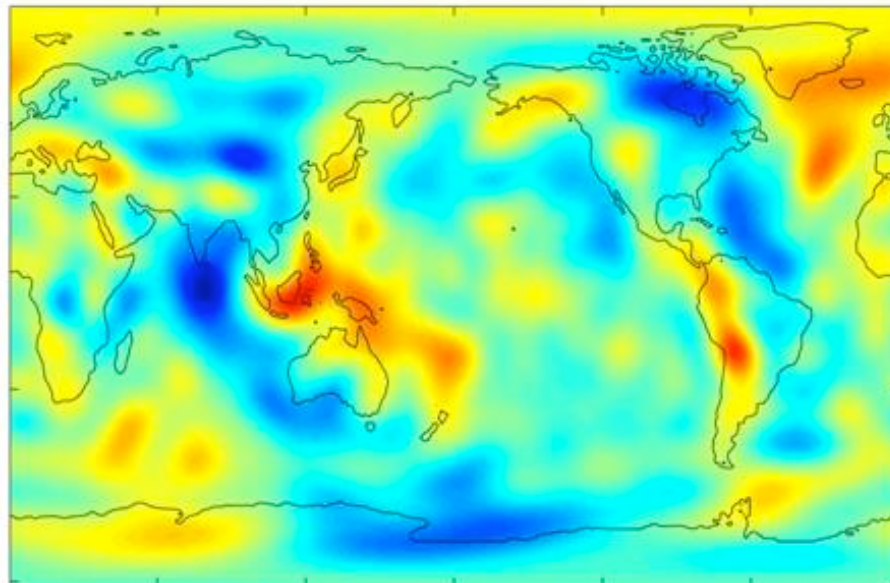
Phase 2 (1998-2003): First power generation units in operation and permanent boat locks. Also, the reservoir will begin to fill to a level of 135 meters.

Phase 3 (2004-2009): Put all generation units into operation. The height of the water will reach 175 meters high.

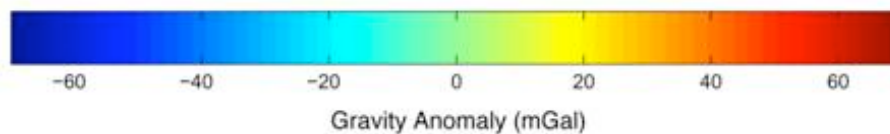


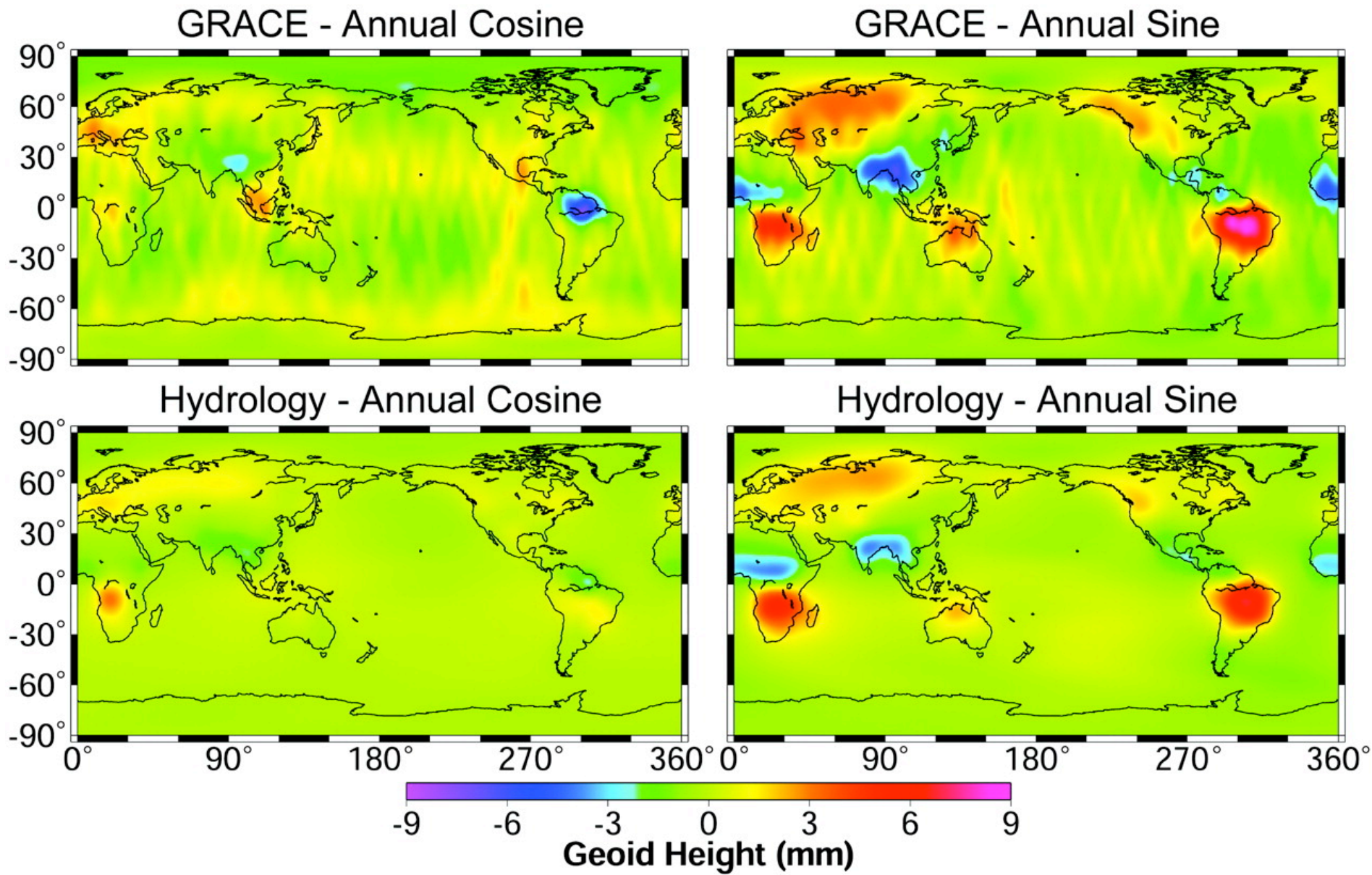


GRACE (2002 -)
gravity map



pre-GRACE (~ 40 years)
gravity map





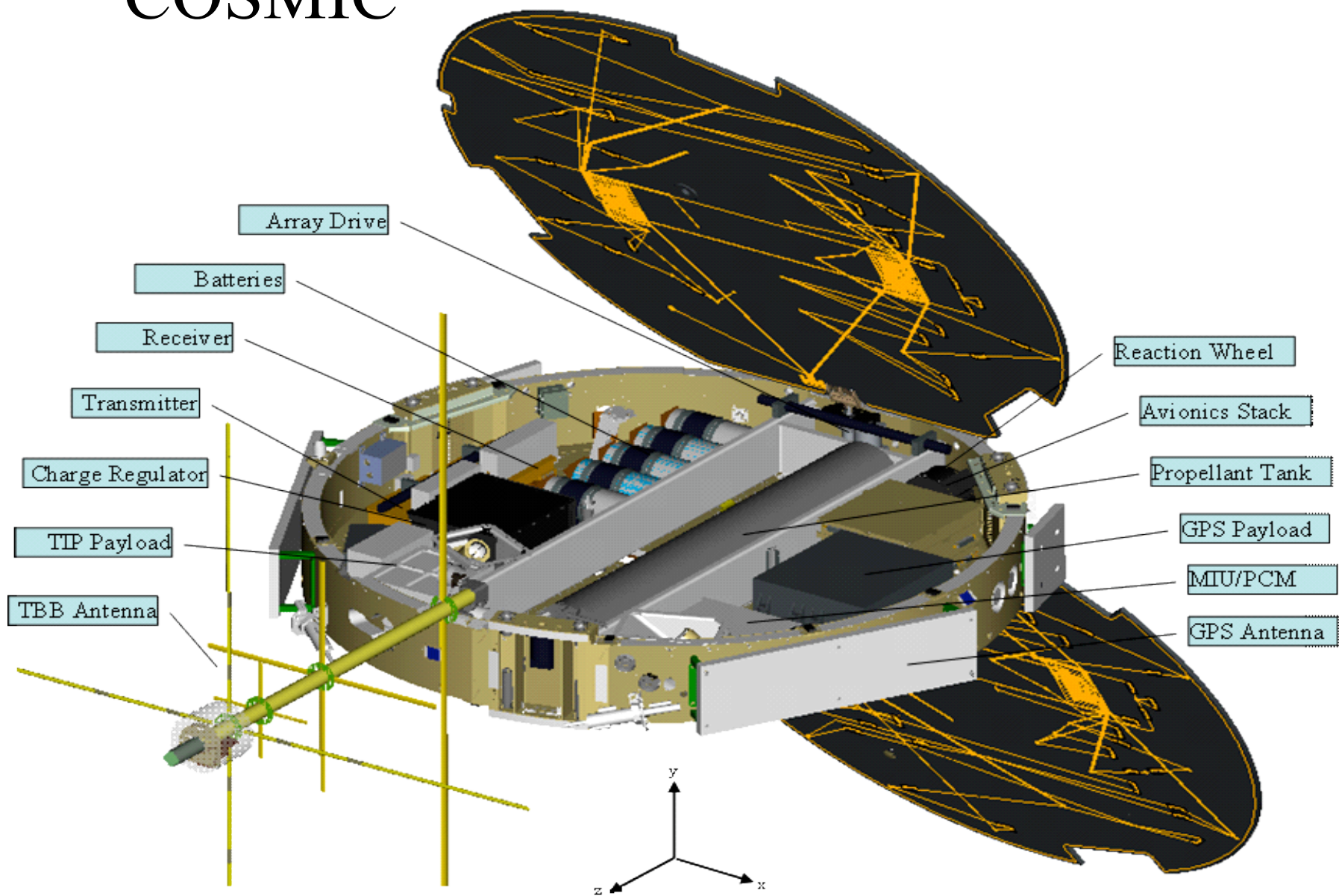
Tapley et al. (2004)

What are troubling GRACE?

(other than “usual” on-board noise sources)

- Nominal **temporal resolution** is too long, ~ 1 month (can tradeoff with precision to ~ 10 days).
- Geophysical signals with period shorter than ~ 1 month become **aliasing errors**: atmospheric pressure, oceanic mass transports, tides, hydrological mass...
- **Spatial resolution** hardly finer than ~ 500 km, realistically 1000-1500 km.
- Wishful **accuracy in surface mass variation** is sub-cm equivalent water thickness for the above spatial and temporal resolution, but realistically > 1 cm.

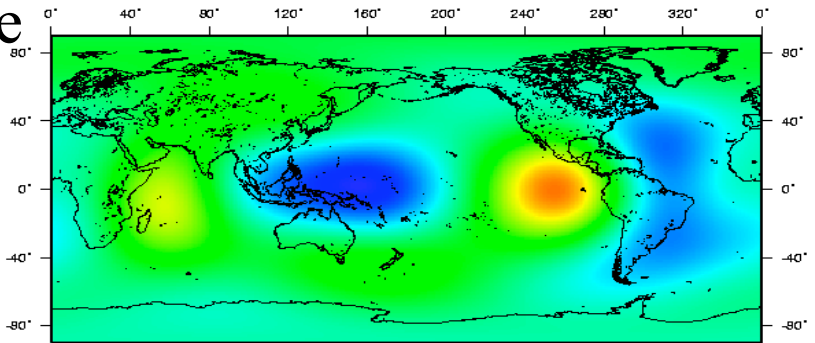
COSMIC



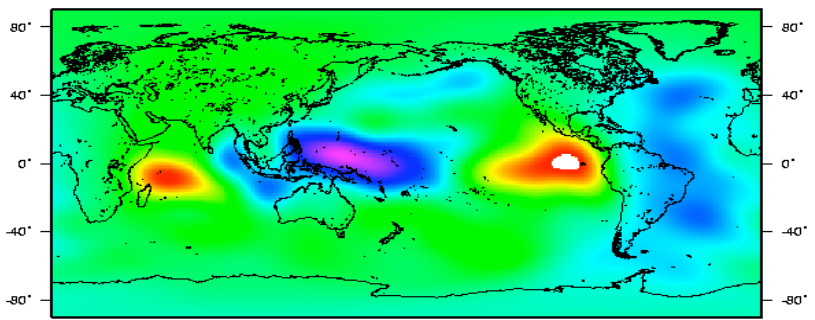
Geoid change due to 1997-1998 El Niño.

harmonic
degree

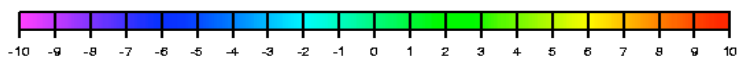
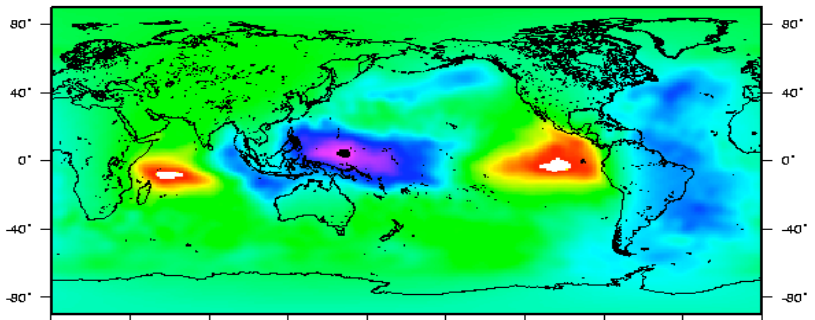
5



15



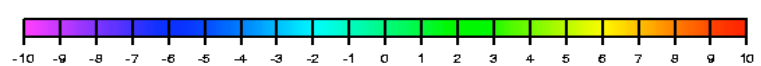
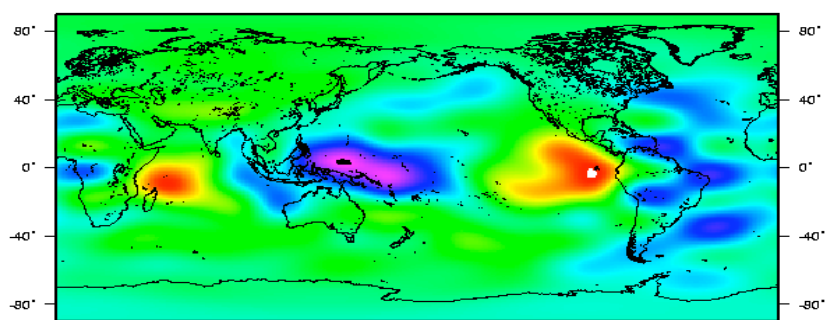
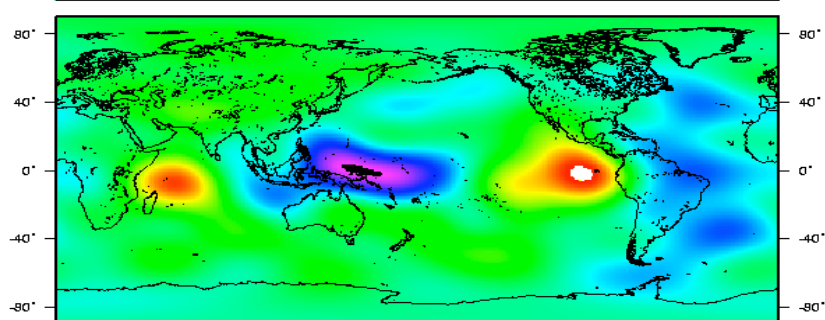
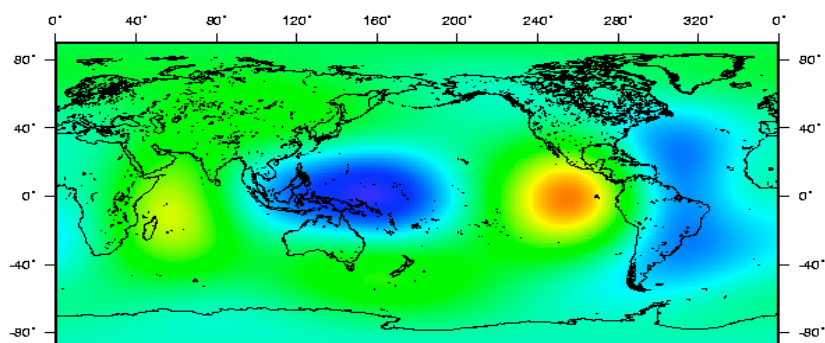
50



mm

Input "data"

(Hwang, 2005)



mm

Simulated "recovery"
by 1-week of COSMIC data

Gravity from COSMIC

- **Orbit**
 - Number (+) (6 after differential nodal precession)
 - Altitude (–,+) (800 km, attenuation)
 - Inclination (+,–) (71°, polar hole)
- **POD data** amount & homogeneity (+)
- **Spatial sampling** (+) (6 orbit plans)
- **Temporal resolution** (+) (6 orbit plans)
- **Accuracy** limitations
 - No accelerometer for non-gravitational force correction (–)
 - GPS/LEO orbit errors and data noise (–)
- **Time span**
 - Relative to GRACE etc. (–,+)
 - Solar max/min (+)
- **Latency**: week-months (?)